XML 查询模式发掘^{*}

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Discovering Frequent Tree Patterns from XML Queries

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Abstract: With XML being the standard for data encoding and exchange over Internet, how to manage XML data efficiently becomes a critical issue. An effective approach to improve the performance of XML management systems is to discover frequent XML query patterns and cache their results. Since each XML query can be modeled as a tree structure, the problem of discovering frequent query patterns can be reduced to frequent structure mining. However, mining frequent query patterns is much more complex than simple structure mining since we have to consider the semantics of query patterns. In this paper, we present an approach to discover frequent XML query patterns efficiently. Compared with previous works, our approach is strictly based on the semantics of XML queries, its mining results are more precise, and can be more effectively utilized by caching system.

Key words: pattern tree; frequent pattern; query caching; XML query

摘 要: 随着 XML 的广泛应用,如何高效地处理 XML 查询受到越来越多的关注.发掘频繁使用的查询模式,并缓 存其查询结果是提高查询效率的有效手段之一.由于 XML 查询可以表示为树,因而可以使用频繁结构挖掘 (Frequent Structure Mining)的技术来发掘频繁查询模式.提出一种高效的频繁查询模式发掘方法,同以前的类似工 作相比,所做工作是严格地基于 XML 查询语义的,因而发掘结果更为准确,也更易于使用. 关键词: 模式树;频繁模式;查询缓存;XML 查询

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1 Introduction

As XML prevails over Internet as a medium for data exchange and representation, how to process XML queries efficiently becomes the imperative research issue. Query caching is one of the most promising approaches to reduce the query processing time. By analyzing the user logs, frequently occurred query patterns can be identified and their result can be materialized to improve the system efficiency. How to cache XML query result gains its focus recently^[5,11] and finding the frequent query patterns plays a critical role in a XML caching system.

Frequent structure mining (FSM) is a new direction in the field of data mining that has been intensively studied recently^[1,9,12]. Given a pattern tree (or pattern graph) S and a set of data trees (or data graphs) $D=\{S_1,\ldots,S_n\}$, usually denoted as the transaction database, we say S occurs in D if we can find an element S_i in D such that there is certain mapping relationship between S and S_i . FSM aims to find the pattern trees (or pattern graphs) that occur frequently over the set D. Since XML queries can be modeled as trees, the problem of discovering frequent query patterns can be reduced to FSM. However, mining frequent query patterns is much more complex than the mining of simple structures because of the semantic issues of query patterns.

In this paper, we propose an approach for frequent query pattern mining strictly based on the semantics of XML queries, and present several techniques to optimize the mining process. Through utilization of the rightmost occurrences of pattern trees in the transaction database, we prove that in order to obtain the frequencies of pattern trees, only single branch pattern trees need to be matched against the transaction database, and the frequencies of multi-branch pattern trees can be figured out through reuse of intermediate results. Experiments show that our method results in substantial performance gains.

The rest of the paper is organized as follows. Basic concepts used in this paper are given in Section 2. Section 3 describes the candidate enumeration method used in this paper. Section 4 presents our approach to discover frequent query patterns. Section 5 gives the results of the experiment study; Section 6 discusses the related works, and we conclude in Section 6.

2 Problem Statement

In this paper, we consider selection patterns in the syntax of XPath^[4], a popular pattern language that are generally modelled as query pattern trees^[7].

Definition 1 (Query Pattern Tree). A query pattern tree is a rooted tree $QPT = \langle V, E \rangle$, where V is the vertex set, E is the edge set. The root of the query pattern tree is a distinguished node denoted by root(QPT). Each vertex v has a label, denoted by v.label, whose value is in {"*"} \cup tagSet, where the tagSet is the set of all element names in the context. A distinguished subset of edges representing ancestor-descendant relationships is called descendant edges.

Figure 1 (a)-(d) shows three QPTs QPT_1 , QPT_2 , and QPT_3 . Descendant edges are shown with dotted lines in diagrams. In what follows, given a query pattern tree $QPT=\langle V,E\rangle$, sometimes we also refer to V and E with QPT if it's clear from the context. Given an edge $e=(v_1,v_2)\in QPT$ where v_2 is a child of v_1 , sometimes v_2 will be denoted as a d-child of v_1 if e is a descendant edge, and as a c-child otherwise. Given two c-children (or d-children respectively) of a QPT node, we say they are duplicate siblings if they share the common label l.



Given a query pattern tree QPT, a rooted subtree RST of QPT is a subtree of QPT such that root(RST)=root(QPT) holds. One of rooted subtrees of QPT₁ is shown in Fig.2(a). Given a tree node $v \in QPT$,

subtree(v) denotes the subtree $T = \langle V', E' \rangle$ of QPT rooted at v. Let QPT be a pattern tree, the size of QPT is defined by the number of its nodes |QPT|. An RST of size k+1 will be denoted as a k-edge RST sometimes. An RST will also be denoted as a single branch RST if it has only one leaf node, and as a multi-branch RST otherwise.

To discover frequent query patterns, one important issue is how to test the occurrence of a tree pattern in the transaction database. Intuitively, we need to discover query patterns whose outputs are more likely to be reused by other queries. The topological mapping method, used by most previous works^[1,9], is not applicable to query pattern mining because for query patterns we must take the semantics into account. The subtree embedding approach used by Ref.[12] is too restrictive since it requires the pattern trees preserve ancestor-descendant relationships. In this paper, we use the concept of tree subsumption, a sound (but not complete) approach to test containment of query pattern trees^[7].

Definition 2(Tree Subsumption). Given two QPTs QPT and QPT', QPT is subsumed in QPT', denoted as QPT_QPT', iff there exists a simulation relation sim between nodes of QPT and nodes of QPT', such that:

1) (root(QPT), root(QPT')) esim;

2) v.label = v'.label or v'.label = "*", if $\langle v, v' \rangle \in sim$;

3) if $\langle v_1, v'_1 \rangle \in \text{sim}$ and v_2 is a c-child of v_1 in QPT, there must exist some c-child v'_2 of v'_1 in QPT' such that $\langle v_2, v'_2 \rangle \in \text{sim}$; if $\langle v_1, v'_1 \rangle \in \text{sim}$ and v_2 is a d-child of v_1 in QPT, there must exist some proper descendant v'_2 of v'_1 in

QPT' such that $\langle v_2, v'_2 \rangle \in sim$.



Figure 2 shows the subsumption of RST in QPT₁.

Given a transaction database $D=\{QPT_i | i=1,...,n\}$, we say RST occurs in D if RST is subsumed in a query pattern tree $QPT_i \in D$. The *frequency* of RST, denoted as Freq(RST), is the total occurrence of RST in D, and supp(RST)=Freq(RST)/|D| is its support rate. Given a transaction database D and a positive number $0 < \sigma \le 1$ called the minimum support, mining the frequent query patterns of D means to discover the set of RSTs of D, $F_D=\{RST_1,...,RST_m\}$, such that for each $RST \in F_D$, $supp(RST) \ge \sigma$.

For example, assume that there are three QPTs QPT_1 , QPT_2 , and QPT_3 in the transaction database as shown in Fig.1, and $\sigma = 0.7$, the RST in Fig.2 (a) occurs in three QPTs, thus it's frequent with respect to this database with supp(RST)=3/4 and Freq(RST)=3.

3 Candidate Generation

In our settings, each data tree is a QPT. Given a transaction database $D=\{QPT_i|i=1,...,n\}$, its global query pattern tree G-QPT is constructed by merging all QPTs in D. Figure 3 shows an example of G-QPT obtained from the QPTs in Fig.1 (a), (b), and (c). Note that for each QPT with duplicate siblings $s_1, ..., s_n$ sharing the common label l, we need re-label them with $l^1, ..., l^n$ respectively before the merging process begins, and re-label them back with l after the merging process has finished. Clearly, when duplicate siblings are present, the merging result is not unique. Under such situation we can choose one merging result arbitrarily because it will not influence the succeeding processing.

The nodes of G-QPT can be numbered from 1 to |G-QPT| through a pre-order traversal. Because each node of $QPT \in D$ is merged with a unique node of the G-QPT, each node of QPT has the same number as the corresponding node in the G-QPT. For example, in Figure 1, integers outside of circles are numbers of corresponding tree nodes. After labeling each node with a number, the representation of QPT₂ can be simplified to string format "1, 2, 3, 4, -1, -1, 7, -1, -1" as in Ref.[12]. We will call such



Fig.3 G-QPT

encoding strings as string encodings of QPTs.

As in Ref.[11], in this paper, we only consider pattern trees that are rooted subtrees of some QPTs in the transaction database. Since each QPT is a rooted subtree of the G-QPT, each pattern tree is also a rooted subtree of the G-QPT. We enumerate all candidate RSTs with the schema-guided right most expansion method proposed in

Ref.[11]. It's not difficult to prove that as in Ref.[11], given a k-edge rooted subtree RST^k in equivalence class [RST^{k-1}], each k+1-edge rooted subtree can be generated with two kinds of operations: the right most leaf node expansion (RMLNE) of RST^k, or the join of RST^k and another rooted subtree RST^k' in the same equivalence class (sometimes the join of RST^k and RST^k will be denoted as RST^k \bowtie RST^k'). And all the k+1-edge rooted subtrees will be enumerated in ascending order.

Figure 4 shows an example of candidates generated from the G-QPT in Fig.3. Due to the presence of duplicate-siblings, some RSTs are likely to be enumerated more than once in our settings, which will incur extra expense. For example, in, RSTs "1, 6, -1" and "1, 9, -1" are equivalent RSTs indeed. However, due to the space limitation, we will not consider this issue further and simply process them as different RSTs.





4 Algorithm

In this section we present an Apriori-based algorithm, FQPMiner, to discover frequent RSTs, then propose several techniques to optimize the mining process.

4.1 Discovering of frequent RSTs

The main framework of our algorithm FQPMiner is shown in Figs.5 and Fig.6. In the algorithm, the notation RST^k denotes a k-edge rooted subtree; F_k is a set of frequent k-edge rooted subtrees. Most of the work is finished in the function FQPGen (see Figure 6), which uses the schema-guided rightmost enumeration method to enumerate candidate RSTs level-wise, counts the frequency of each candidate RST, and prunes infrequent RSTs based on the anti-monotone property of tree subsumption.

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Algorithm:FQPMiner(D,minSupp)

Input: D—transaction database

minSupp—the minimum support

Output: the set of all frequent RST sets

(1)F_1=\{1-\text{edge rooted subtrees in }D\};

(2)for(k=1; F_k \neq b; k++) \text{ do}

(3) F_{k+1}=FQPGen(F_k, \min \text{Supp}, D);

(4)\text{return } \{F_i | i=1,...,k-1\};

Fig.5 Algorithm to find frequent RSTs
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To count the frequency of an RST, a naive solution is to match it against each QPT in the transaction database. This method will be very inefficient because tree matching is expensive. FQPGen can count the supports of candidates more efficiently through utilization of transaction IDs. For each RST, FQPGen maintains a TIDList attribute that contains transaction IDs of QPTs in which the RST occurs. We can easily prove that an RST is subsumed in a QPT only if all its rooted subtrees are subsumed in the QPT. Hence, only 1-edge RSTs need to be matched against each QPT in the transaction database. To count the frequency of a k-edge RST RST^k (k>1), if RST^k is a single-branch RST, FQPGen need only to match RST^k against QPTs whose transaction IDs are in the set RST^{k-1}.tidlist, where RST^{k-1} is the k-1-edge RSTs that is a rooted subtree of RST^k (lines 4-7 of Fig.6). If RST^k is a multi-branch k-edge RST, then FQPGen need only to match RST^k against QPTs whose transaction IDs are in the set

In the algorithm, Contains (lines 6, 12, and 17) is a function based on the definition of tree subsumption in Section 3. The basic idea is to look for a simulation between two trees by constructing a relation R and then removing from R all pairs (u,u') that will violate condition (3) of the definition of tree subsumption. We will not give its detail because of its strong resemblance with the algorithm presented in Ref.[7].

Algorithm: FQPGen (F_k , minSupp, D) Input: D: transaction database minSupp: the minimum support F_k : the set of frequent k-edge RSTs Output: the set of all frequent RST sets (1) $F_{k+1} = \phi;$ (2) for each rst $\in F_k$ for each rst' obtained by expansion of rst (3) (4) if rst' is a single-branch RST for each transaction $t \in D$ such that $t.tid \in rst.tidlist$ do (5) if Contains(t, rst') (6) rst'.tidlist←t.TID; (7) if rst' is a multi-branch RST generated through RMLNE (8) (9) obtain RST_k by cutting off one leaf of rst'; $tempList = rst.tidlist \cap RST_k.tidlist;$ (10)for each transaction $t \in D$ such that $t.tid \in tempList$ do (11)if Contains(t, rst') (12)(13) rst'.tidlist←t.TID; if rst' is generated through join of rst and RSTk (14) $tempList = rst.tidlist \cap RST_k.tidlist;$ (15) for each transaction $t \in D$ such that $t.tid \in tempList$ do (16) if Contains(t, rst') (17) (18) rst'.tidlist←t.TID; if $(|rst'.tidList| \ge minSupp)$ (19) (20) $F_{k+1} \leftarrow rst;$ (21) return F_{k+1}; Fig.6 Candidate generation algorithm

4.2 Optimization

In this subsection, we propose a technique for further optimization of the mining process. We prove that through utilization of rightmost occurrences, multi-branch RSTs needn't be matched against QPTs even in our settings.

Definition 3 (Proper Combination). Given an rooted subtree RST and a query pattern tree QPT, where $\langle v_1, ..., v_m \rangle$ is the set of nodes of RST sorted in pre-order, assume that RST \subseteq QPT holds and sim is the simulation relation between their nodes, then the *Proper Combinations* of sim is the set PC= $\{\langle v'_1, ..., v'_m \rangle | v'_i \in V', i=1, ...,m\}$ such that for each $\langle v'_1, ..., v'_m \rangle \in PC$: if v_j is a c-child of v_k , v'_j must be a c-child of v'_k ; if v_j is a d-child of v_k , v'_j must be a proper descendant of v'_k , where *j*, *k* are any integers such that $1 \leq j, k \leq m$ holds.

Definition 4 (Rightmost Occurrence). Given an rooted subtree RST and a query pattern tree QPT where the list $L = \langle v_1, ..., v_m, ..., v_k \rangle$ is the set of nodes of RST sorted in pre-order, v_m and v_k is the second rightmost leaf and the rightmost leaf of RST respectively, assume that RST \subseteq QPT holds, sim is the simulation relation between their nodes, then the *rightmost occurrence* of RST in QPT is the set rmo(RST,QPT)= $\{\langle v'_m, v'_k \rangle | \langle v'_m, v'_k \rangle$ is a sub-list of some proper combination $\langle v'_1, ..., v'_m, ..., v'_k \rangle$ of sim $\}$. Note that if the RST has only one leaf node, then the first element of its rightmost occurrence of RST in D is the set rmo(RST,D)= $\{\langle u, v, \{QPT.tid | for all QPT \in D \text{ such that } \langle u, v \rangle \in rmo(RST, QPT)\}\}$

Definition 5 (Conditional Rightmost Occurrence). Given a rooted subtree RST and a query pattern tree QPT,

where $\langle v_1, ..., v_i, ..., v_m \rangle$ is the set of nodes of RST sorted in pre-order, and v_i is a node of the rightmost branch of RST, assume that RST QPT holds, sim is the simulation relation between their nodes, and $\langle v_i, v' \rangle \in sim$, we define the *Conditional Rightmost Occurrence* satisfying $\langle v_i, v' \rangle \in sim$ as the set $\{v'_m \mid \text{there exists a proper combination of sim}$ $\langle v'_{1}, ..., v'_{ij}, ..., v'_{ij} \rangle$ such that $v'_i = v'$. We denote it as $\operatorname{rmo}_{\langle v_i, v' \rangle \in sim}(RST, QPT)$.

For example, given the transaction database composed of QPT_1 , QPT_2 , and QPT_3 as shown in Fig.1 (assume 1, 2, and 3 are their respective transaction IDs), and the global query pattern tree G-QPT in Fig.3, if sim is the simulation relation between RST "1, 2, 3, -1, 7, -1, -1" and G-QPT, then the proper combinations of sim are { $\langle 1, 2, 3, 5 \rangle$, $\langle 1, 2, 3, 7 \rangle$ }, the rightmost occurrence of the RST in G-QPT will be { $\langle 3, 5 \rangle$, $\langle 3, 7 \rangle$ }, the rightmost occurrence of the RST in the transaction database will be { $\langle 3, 5, \{1\} \rangle$, $\langle 3, 7, \{2\} \rangle$ }. Clearly, the frequency of an RST freq(RST) = [{tid|tid \in TIDList, $\langle u, TIDList \rangle \in rmo(RST, D)$ }.

Lemma 1. Given a transaction database D, its global query pattern tree G-QPT, and two k-edge RSTs RST₁, RST₂ \in [RST^{k-1}], let RST^{k+1}= RST₁ \bowtie RST₂, p is the node of RST^{k+1} not present in RST₁ (i.e., the rightmost leaf of RST₂), and the junction node q is parent of p, then we have:

1) If RST₁ is a single branch RST, then rmo(RST^{k+1}, D) = { $\langle u, u', \text{TIDList}_1 \cap \text{TIDList}_2 \rangle$ $\langle v, u, \text{TIDList}_1 \rangle \subseteq \text{rmo}(\text{RST}_1, D), \langle v', u', \text{TIDList}_2 \rangle \subseteq \text{rmo}(\text{RST}_2, D)$, where $u \in \text{rmo}_{\langle q, q' \rangle \in \text{sim}}(\text{RST}_1, \text{ G-QPT}), u' \in \text{rmo}_{\langle q, q' \rangle \in \text{sim}}(\text{RST}_2, G)$ G-QPT, and $q' \in \text{G-QPT}$ }.

2) If both RST₁ and RST₂ are multi-branch RSTs, and the parent of the rightmost leaf of RST₁ has only one child, then $rmo(RST^{k+1},D)=\{\langle u, u', TIDList_1\cap TIDList_2\rangle\} \langle v, u, TIDList_1\rangle \subseteq rmo(RST_1, D), \langle v', u', TIDList_2\rangle \subseteq rmo(RST_2, D), u << v', where <math>u \in rmo_{< q, q'>esim}(RST_1, G-QPT), u' \in rmo_{< q, q'>esim}(RST_2, G-QPT), and q' \in G-QPT \}$. Here u << v' means v' is the parent (or ancestor respectively) of u if the rightmost leaf of RST₁ is a c-child (or d-child respectively) of its parent.

1) Otherwise, $\operatorname{rmo}(\operatorname{RST}^{k+1}, D) = \{\langle u, u', \operatorname{TIDList}_1 \cap \operatorname{TIDList}_2 \rangle | \langle v, u, \operatorname{TIDList}_1 \rangle \subseteq \operatorname{rmo}(\operatorname{RST}_1, D), \langle v', u', \operatorname{TIDList}_2 \rangle \subseteq \operatorname{rmo}(\operatorname{RST}_2, D), u = v', \text{ where } u \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{sim}}(\operatorname{RST}_1, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{sim}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{sim}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{sim}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{sim}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{sim}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{sim}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{sim}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{sim}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{sim}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{sim}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{sim}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{sim}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{sim}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{sim}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{sim}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{sim}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{sim}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{rmo}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{rmo}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{rmo}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{rmo}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{rmo}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{rmo}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}_{\langle q, q' \rangle \in \operatorname{rmo}}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in \operatorname{rmo}(\operatorname{RST}_2, \operatorname{G-QPT}), u' \in$

Lemma 1 can be proved based on the definition of tree subsumption. We will not give the detail due to space limitation. Based on Lemma 1, all RSTs generated through join operations are not required to match with QPTs. Now we turn to investigate RSTs generated through rightmost leaf node expansion.

Lemma 2. For any multi-branch k+1-edge rooted subtree RST^{k+1} generated through rightmost leaf node expansion of a k-edge rooted subtree RST_1 , there must be another k-edge rooted subtree RST_2 which is formed by cutting off the second rightmost leaf node of RST^{k+1} such that the join of RST_1 and RST_2 will produce RST^{k+1} itself. If RST_2 exists in F_k , then we have: $rmo(RST^{k+1}, D) = \{\langle v, u', TIDList_1 \cap TIDList_2 \rangle | \langle v, u, TIDList_1 \rangle \subseteq rmo(RST_1, D), \langle v', u', TIDList_2 \rangle \subseteq rmo(RST_2, D), u' << u\}$, otherwise, RST^{k+1} must be infrequent.

Based on Lemma 1 and Lemma 2, we have the following result:

Theorem 1. By using the rightmost occurrence of RST in D, only those single-branch RSTs need to be matched with QPTs. The frequencies of other RSTs can be computed through reusing intermediate results.

Based on the above discussion, we are in a position to describe our algorithm FQPMinerRMO. Its main framework is similar to FQPMiner, but the candidate generation algorithm FQPGen is adapted into FQPGenRMO in Fig.7. FQPGenRMO associates each RST with its rightmost occurrence in the transaction database. Lines 6-7 deal with single-branch RSTs. We use GetRMO algorithm to match single-branch RSTs against QPTs to obtain their rightmost occurrences (line 7). GetRMO is an extension to Contains algorithm used in FQPMiner, but its detail is not included in this paper. Lines 8-12 cope with multi-branch RSTs generated through RMLNE using Lemma 2, Lines 13-17 handle RSTs generated through join using Lemma 1. For simplification of representation, only case (1) of Lemma 1 is illustrated in Fig.7. Line 18 obtains TIDList of a rooted subtree from its rightmost occurrence. Lines

19-20 check whether the result subtree is frequent, and those frequent ones are added as members into F_{k+1} .

While expanding an n-edge RST rst_n to generate an n+1-edge RST rst_{n+1}, we obtain the rightmost occurrence rmo(rst_{n+1}, D) through computation over rmo(rst_n, D) and rmo(rst'_n, D), where rst'_n is another n-edge RST. We can prove that rst_n \leq rst'_n always holds (definition of order relationship \leq can be found in Ref.[11]), it implies that after the expansion of an RST rst_n, its rightmost occurrence rmo(rst_n, D) will not be used, hence, needn't be maintained, any longer. Based on the above discussion, *FQPGenRMO* can remove the rightmost occurrence information as early as possible (line 21), and the memory cost will be reduced drastically.

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Algorithm: FQPGenRMO(Fk, minSupp, D)
Input: D: transaction database
minSupp: the minimum support
        F_k: the set of frequent k-edge RSTs
Output: the set of all frequent RST sets
(1) F_{k+1} = \phi;
(2) for each rst \in F_k
         for each rst' obtained by expansion of rst
(3)
(4)
               rmo(rst', D) = \{\};
(5)
               if rst' is a single-branch RST
(6)
                     for each transaction t \in D such that t.tid \in rst.tidlist do
(7)
                           rmo(rst', D) = rmo(rst', D) \cup \{GetRMO(rst', t)\}
(8)
               if rst' is a multi-branch RST generated through RMLNE
                     obtain RST<sub>k</sub> by cutting off the second rightmost leaf of rst';
(9)
(10)
                     for each pair (\langle v, u, tidlist_1 \rangle \in rmo(rst, D), \langle v', u', tidlist_2 \rangle \in rmo(RST_k, D))
(11)
                           if u' << u
(12)
                                 rmo(rst', D) = rmo(rst', D) \cup \{ < v, u', tidlist_1 \cap tidlist_2 > \};
(13)
               if rst' is generated through join of rst and RST_k, and j is the junction node
                     GetCondRMO(rst, G-QPT, j, rmo(rst, G-QPT), cond-rmo);
(14)
(15)
                     GetCondRMO(RSTk, G-QPT, j, rmo(RSTk, G-QPT), cond-rmok);
                     for each q such that \langle q, u \rangle \in cond-rmo, \langle q, u' \rangle \in cond-rmo<sub>t</sub>
(16)
                           rmo(rst', D) = rmo(rst', D) \cup \{ < u, u', tidlist_1 \cap tidlist_2 > \}
(17)
                                    \langle v, u, tidlist_1 \rangle \in rmo(rst, D), \langle v', u', tidlist_2 \rangle \in rmo(RST_k, D);
(18)
               rst'.tidlist={t.TID| t.TID e tidlist<sub>1</sub>, <p, tidlist<sub>1</sub>> e rmo(rst', D)};
(19)
               if (|rst'.tidList| \ge \min Supp)
(20)
                     F_{k+1} \leftarrow rst';
               remove rmo(rst, D);
(21)
(22)
               remove rst.tidlist;
(23) return F_{k+1};
```

Fig.7 Utilization of rightmost occurrences

Figure 8 shows the algorithm GetCondRMO, which are used for the computation of the rightmost occurrences of those RSTs generated through join operation (line 14-15 of Fig.7). GetCondRMO obtains the conditional rightmost occurrences of an RST in the G-QPT. GetCondRMO uses post-order enumeration of the nodes in RST. The main loop visits RST nodes in descending order (see line 2 of Fig.8). Assume q is the current RST node. The algorithm fetches all G-QPT nodes with the same label value as q (line 4). For each fetched node d of the G-QPT, the algorithm try to match subtree of RST rooted at q against subtree of the G-QPT rooted at d. Since subtrees of RST rooted at the child nodes of q have already been matched in preceding loops, the algorithm need only to check whether for each c-child node (or d-child node respectively) q' of q, there is a c-child (or descendant) d' of d, such that q' and d' are matched in preceding loops (line 6-13). RST is matched with the G-QPT if the root of RST is matched with the root of the G-QPT at the ending point (line 25). For each node d of the G-QPT that is matched with an ancestor node q of the rightmost leaf node (or junction node respectively) of RST, the ancestor-descendant relationship between d and d' is recorded (line 16-23), where d' is a node of the G-QPT that will be matched with the rightmost leaf node (or junction node respectively) of RST when d is matched with q. The ancestor-descendant relationship between d and d' will at last be used to obtain conditional rightmost occurrence (line 25-26).

5 Experiments

In this section, we present experimental results to evaluate the effectiveness of our algorithm on a range of datasets and parameters. All experiments were performed on a 1.8GHz PC with 512MB RAM, running Windows 2000 Server. The algorithms were implemented in C^{++} .

Algorithm: GetCondRMO(RST, G-QPT, c, rmo, cond-rmo) Input: RST: a rooted subtree G-QPT: the global pattern tree c: the junction node of RST rmo: the rightmost occurrence of RST in GQPT cond-rmo: the conditional rightmost occurrence (used for returning result) Output: the conditional rightmost occurrence (1)rml.match = rmo; //rml is the rightmost leaf of RST (2) for all other $q \in RST$ //iterate all nodes of RST except for rml in postorder (3)q.match = $\{\};$ (4) for all $d \in G$ -QPT such that d. label = q. label (5) new map_d; for all $q' \in children(q)$ (6) (7) $map_{d}q' = \{\};$ (8) if q' is a d-child (9) for all $d \in q'$.match such that d is an ancestor of d' $map_{d}q' = map_{d}q' \cup \{d'\};$ (10)(11)if q' is a c-child (12)for all $d' \in q'$.match such that d' is a c-child of d(13) $map_d.q' = map_d.q' \cup \{a''\};$ (14) if not exist p such that map_d.p = {} q.match = q.match \cup {d}; (15) (16) if q is parent of the rightmost leaf (17) d.rmo = map_d.rml; (18)if q is c or a descendant of cand an ancestor of the rightmost leaf except for its parent (19) $d.rmo = \{p | p \in q.rmo, q \in map_d.rmc\};$ (20)if q is parent of c (21) d.cond = map_d.rmc; (22)if q is an ancestor of c except for its parent (23) $d.cond = \{m \mid m \in n.cond, n \in map_d.rmc\};$ (24) delete map_d; (25) if q is the root of RST and d is the root of G-OPT (26)cond-rmo = cond-rmo $\cup \{ < m, n > | m \in d.cond, n \in m.rmo \};$ (27)return;

Fig.8 The algorithm to obtain the conditional rightmost occurrence

We use DBLP.dtd as the schemas of XML data sources. Given a DTD, we first construct a G-QPT by introducing duplicate siblings, descendant edges, and wildcards. Then we generate all RSTs of the G-QPT, and use Zipf and uniform distribution of RSTs to produce the transaction file of QPTs. Zipf distribution is used since Web queries and surfing conform to Zipf's law^[3], while uniform distribution is used only to see what differences might happen to our approaches with different QPT distribution. The characteristics of each dataset are listed in Table 1. A RST with descendant edges takes more time to compare with QPTs than a RST without descendant edges. Consequently, the number of descendant edges in G-QPT tells the difficulty of tree matching. On the other hand, the average number of nodes, maximum depth and fanout of QPTs also show the complexity of the dataset.

Datasets	G-QPT				QPT in DB			DB size of
	#of nodes	Max depth	#of d-child	Max fanout	Avg # of nodes	Max depth	Max fanout	100K dataset (KB)
Zipf	98	8	24	12	7.4	8	12	3549
Uniform	98	8	24	12	9.2	. 8	12	4843

Two groups of experiments are performed. The first group of experiments is to show the performance of our

algorithms at a range of different minimum support values. We use 100K datasets, which contain 100,000 QPTs. The second group aims to present the scale-up of our algorithms at minimum support value 1%. The total number of QPTs in each datasets ranges from 50K, 100K, 200K, 300K to 500K.

The performance of FQPMiner and FQPMinerRMO is shown in and. For 100K data set of Zipf distribution, FQPMinerRMO is 5-7 times faster than FQPMiner. The reason is that FQPMiner will match each candidate RST against QPTs in the transaction database while FQPMinerRMO processes the majority of candidate RSTs without matching operation. In addition, matching time of single-branch RSTs is much less than that of multi-branch RSTs. Consequently, FQPMinerRMO takes much less time than FQPMiner. This fact is further confirmed in the data set of uniform distribution, where FQPMinerRMO can be 8-12 times faster than FQPMiner.



Fig.10 Experiment results

The result of scale-up experiment is shown in. At a given minimum support value 1%, we performed the experiments by varying the number of transactions(QPTs) in database file DBLP(Zipf) from 50,000 to 500,000. From the, we find that the execution time of both FQPMinerRMO and FQPMiner algorithms scales almost linearly with the size of dataset. Meanwhile, we also find that FQPMinerRMO continues to be about 5-7 times faster than FQPMiner. This fact is further confirmed in the data set of uniform distribution (see), where FQPMinerRMO continue to be 8-10 times faster than FQPMiner.

6 Related Work

Data mining is an important research area in the field of knowledge engineering. Recently researchers gradually shift their focus to mining frequent structures like graphs^[6,9] or trees^[8,12,1,10,11]. Different from our work, most previous works assume that transaction database is consisted of simple trees or graphs without descendant edges or wildcards, and their methods are not directly applicable to our applications since they can't handle special

XPath constructs, which would make the computation much more complex.

Reference [12] is more closely related with our works. In its settings, each edge works as a descendant edge. It maintains prefix matches for each candidate pattern, and proposed a method to compute the prefix matches of k+1-edge patterns from prefix matches of k-edge patterns incrementally. Since the support counts of candidate patterns can be derived their prefix-matches, Ref.[12] can get the support counts of candidate patterns without matching them against transactions. However, under special cases, the memory cost of prefix matches of a candidate could be exponential to its size. For instance, given a transaction tree DT composed of a chain of n nodes and a pattern tree PT composed of a chain of m+1 nodes, where each node is labeled with the same label l, Ref.[12] has to maintain n!/((n-m)!*m!) prefix matches for the match between PT and DT. Clearly, the algorithm of Ref.[12] is intractable since they have to generate and compare each prefix matche.

The discovering of frequent XML query patterns was initially proposed in Refs.[10,11]. In Refs.[10,11], several efficient algorithms are proposed through utilization of tidLists. However, Refs.[10,11] utilize tidLists based on the following assumption: if all proper subtrees of a multi-branch pattern tree occur in a data tree, then the pattern tree itself must also occur in the data tree. The above assumption may lead to imprecise mining results because based on the semantics of XML queries, it doesn't hold under certain special cases. For example, although each proper rooted subtree of RST_2 in Fig.11 is subsumed in QPT₅, RST_2 itself is not.



7 Conclusions

In this paper, we present an efficient algorithm to discover frequent rooted subtrees from XML queries through utilization of rightmost occurrences. Our method is strictly based on the semantics of XML queries, and we believe this is very important for effective utilization of the mining results.

Future work includes incremental computation of frequent RSTs. To incorporate the result of this paper into caching system, an important issue is to guarantee the freshness of the materialized data. The caching system must guarantee the consistence of the mining result with the history database D. However, if the pattern of user activity changes at a relatively high rate, the accuracy of the mining result may deteriorate fast. Because re-computation will incur a high overhead, finding a method to discover frequent RSTs incrementally becomes very important.

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